

Take Home Quiz 5 KEY

Take home quizzes are due at the beginning of the following lecture. They are worth 2 points of EXAM credit. Please attach this sheet to your answers if additional sheets are used.

1. Figure 7.19 in the text shows the dry ($P_{\text{H}_2\text{O}} = 0$) and the wet ($P_{\text{H}_2\text{O}} = P_{\text{fluid}}$) cases. Use the Clapeyron equation to explain the following:

- A. For the dry case, why the slope of dP/dT is positive.
- B. For the wet case, why the slope of dP/dT is negative.
- C. For the wet case, below $P = 0.15$ GPa, why the curve shows a large initial depression of the melting point.
- D. For the wet case, above $P = 0.15$ GPa, why the slope of the line is much less negative.

1A. The Clapeyron equation is

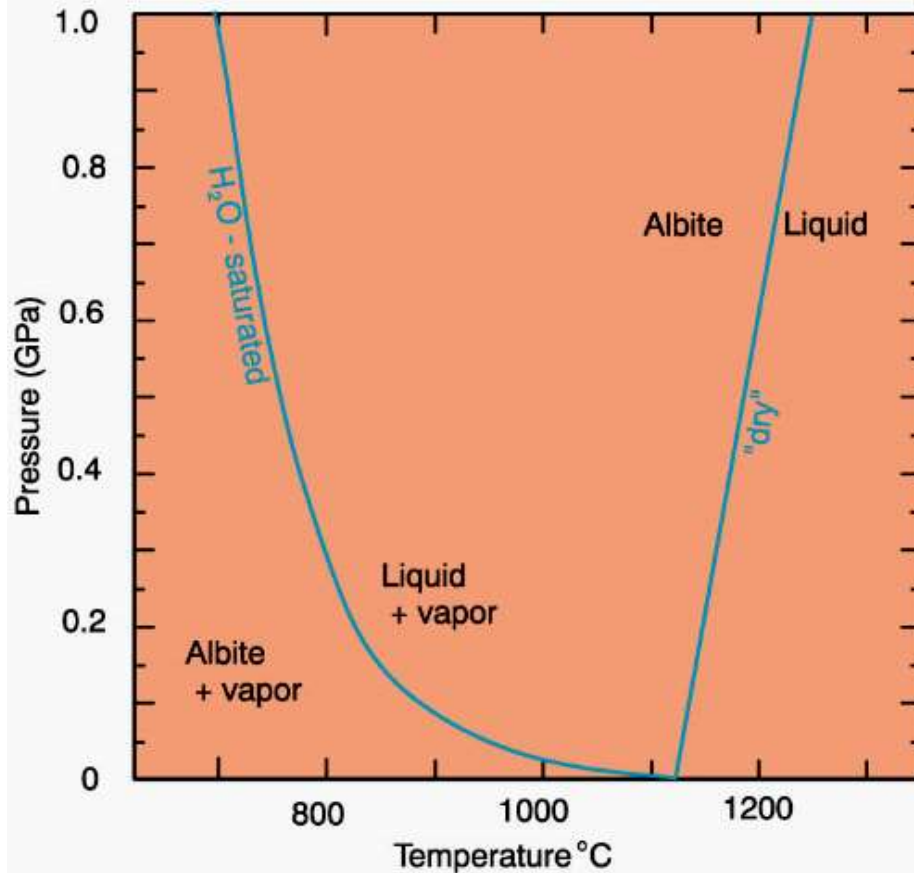
$$\frac{dP}{dT} = \frac{\Delta S}{\Delta V}$$

For the transition from solid to liquid, entropy increases, so ΔS is positive. The volume also increases on going from solid to liquid. Since both ΔS and ΔV are positive, dP/dT must be positive.

1B. For the equation,



volume decreases on going from vapor to liquid, so ΔV is negative. This means the dP/dT is negative.



1C. Below 0.15 GPa, the gas volume decreases rapidly with increasing pressure, so ΔV is negative and large. Thus, there is a substantial depression of the melting point. It is the rate of change of ΔV with P that is important. Mathematically,

$$\left(\frac{(\delta\Delta V)}{(\delta P)} \right)_T$$

1D. Above 0.15 GPa, the gas volume continues to shrink with increasing pressure, but at a much smaller rate. Thus, the melting point depression with increasing pressure is more gradual. ΔV is still negative, but the rate of change is smaller.